

Figure 2

A town's population, P, is modelled by the equation  $P = ab^t$ , where a and b are constants and t is the number of years since the population was first recorded.

The line l shown in Figure 2 illustrates the linear relationship between t and  $\log_{10} P$  for the population over a period of 100 years.

The line *l* meets the vertical axis at (0, 5) as shown. The gradient of *l* is  $\frac{1}{200}$ .

(a) Write down an equation for *l*.

(2)

(b) Find the value of a and the value of b.

(4)

- (c) With reference to the model interpret
  - (i) the value of the constant a,
  - (ii) the value of the constant b.

**(2)** 

- (d) Find
  - (i) the population predicted by the model when t = 100, giving your answer to the nearest hundred thousand,
  - (ii) the number of years it takes the population to reach 200 000, according to the model.

(3)

(e) State two reasons why this may not be a realistic population model.

(2)